# Frontier Topics in Empirical Economics: Week 7 Bartik Instruments

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#### Introduction

- We have already learned some basic IV methods and their extensions
- Today we will investigate a particular type of IV
- Bartik instrument, or shift-share instrument (SSIV)
- It is widely used in different contexts
- Especially trade and migration (spatial economics)
- How should we use it? What is its regression assumption?

#### Introduction

- We will introduce two different frameworks of this instrument
  - Goldsmith-Pinkham, Sorkin, and Swift (2020) consider share as IV, shift as weight
  - Borusyak, Hull, and Jaravel (2022) consider shift as IV, share as weight
- You can validate your regression by proving either set of assumptions are correct
- It depends on your context

# Motivating Example: Card (2009)

- Let's start with an example from Card (2009)
- What is the impact of immigrant ratio on native-immigrant wage gap?

$$y_I = \beta_0 + \beta \ln x_I + \beta_2 C_I + \epsilon_I \tag{1}$$

- *I* is location, *y* is log wage gap between immigrants and natives, *x* is ratio of immigrant labor to native labor, *C* is location-level control
- $\blacksquare$  x is endogenous: Some positive productivity local shock affects both x and y

# Motivating Example: Card (2009)

- Let's use an IV for x
- We have data for 1980,1990, and 2000
- We construct a shift-share IV  $B_I$  as follows:

$$B_{I} = \sum_{k} \underbrace{Z_{Ik,1980} \cdot g_{k}}_{share} \cdot \underbrace{g_{k}}_{shift} \tag{2}$$

$$Z_{lk,1980} = (N_{lk,1980}/N_{k,1980}) \times (1/P_{l,2000})$$
 (3)

- k is home country,  $N_{Ik,1980}$  is the number of immigrants in I from k in 1980,  $P_{I,2000}$  is population in I in 2000
- $Z_{lk,1980}$  evaluates the base year share of immigrants from k in l
- $g_k$  is the number of people arriving the US from 1990 to 2000 from k

#### Motivating Example: Card (2009)

- What is the basic idea of this IV?
  - (1) Relevance: Clustering of immigrants from the same country (Chinese in SF)
  - (2) Exclusion: The local exposure of the national shock is not related to other local shocks
- It decomposes local immigrant into local-origin country
- This is an instrument with "Local Share" × "National Growth (Shift)"
- We call this shift-share/Bartik instrument

# Motivating Example: Autor, Dorn, and Hanson (2013)

- Another important example is Autor, Dorn, and Hanson (2013) on China shock
- What is the impact of China's import on local labor market in the U.S.?
- They construct a shift-share variable as follows:

$$\Delta IPW_{it} = \sum_{j} \frac{L_{ijt}}{L_{jt} \cdot L_{it}} \Delta M_{jt}$$

- *i* is region, *j* is industry, *t* is year
- $L_{ijt}$  is employment in region i industry j
- **L**<sub>jt</sub> is total employment in industry j in the U.S.
- $\blacksquare$   $L_{it}$  is total employment in region i
- lacksquare  $\Delta M_{it}$  is import growth from China to the U.S. in industry j

# Goldsmith-Pinkham, Sorkin, and Swift (2020): Share as IV

- How to interpret this shift-share IV?
- Let's first investigate Goldsmith-Pinkham, Sorkin, and Swift (2020)
- In this paper, we consider share as IV, shift as weight

# Goldsmith-Pinkham, Sorkin, and Swift (2020): Definition of Bartik IV

- Let's define Bartik IV generally
- We have the following equation

$$y_{lt} = D'_{lt}\rho + x_{lt}\beta_0 + \epsilon_{lt} \tag{4}$$

- *I* is location; *t* is time; *D* are controls;  $\beta_0$  is parameter of interest
- $\mathbf{x}_{lt}$  is some (employment) growth rate
- $y_{lt}$  is some (wage) outcome growth rate
- x and y can also be level variables when location FE is controlled
- We assume that  $x_{lt} \perp \!\!\! \perp \epsilon_{lt}$ , need an IV
- Bartik IV comes from two identities

# Goldsmith-Pinkham, Sorkin, and Swift (2020): Definition of Bartik IV

- Identity 1: Decompose Location-level growth variable to location-industry-level variable and its growth
- Usually location-industry level, or in Card (2009), location-origin country level

$$x_{lt} = Z_{lt}G_{lt} = \sum_{k=1}^{K} z_{lkt}g_{lkt}$$

 $z_{lkt}$  is the location-industry share at t,  $g_{lkt}$  is the location-industry growth at t

 Identity 2: Decompose location-industry growth into national and local components

$$g_{lkt} = g_{kt} + \tilde{g}_{lkt}$$

 $g_{kt}$  is the national industry growth,  $\tilde{g}_{lkt}$  is the location-industry growth shock

## Goldsmith-Pinkham, Sorkin, and Swift (2020): Definition of Bartik IV

- Assume that we have a baseline period 0
- We construct Bartik IV  $B_{lt}$  as:

$$B_{lt} = Z_{l0}G_t = \sum_{k} \underbrace{z_{lk0}}_{Share\ Shift} \underbrace{g_{kt}}_{Sh}$$
 (5)

- The first part is the initial share of industry k in location l
- lacktriangle The second part is the national growth of industry k
- Fix z at 0 and drop  $\tilde{g}_{lkt}$  from the identity  $\Rightarrow$  Bartik IV
- Before we formally establish the equivalence between Bartik IV and GMM
- Let's consider two special cases

- Case 1: Two industries and One period
- Shares sum to 1:  $z_{12} = 1 z_{11}$

$$B_I = z_{I1}g_1 + z_{I2}g_2 = g_2 + (g_1 - g_2)z_{I1}$$

We have the first stage:

$$x_{I} = \gamma_{0} + \gamma B_{I} + \eta_{I} = \underbrace{(\gamma_{0} + \gamma g_{2})}_{constant} + \underbrace{\gamma(g_{1} - g_{2})}_{coefficient} z_{I1} + \eta_{I}$$

• Using Bartik in 2SLS is identical to using single IV,  $z_{l1}$ 

Case 2: Two industries and Two periods

$$B_{lt} = g_{1t}z_{l10} + g_{2t}z_{l20} = g_{2t} + (g_{1t} - g_{2t})z_{l10}$$

Assume that we control for time FE, we have a first stage:

$$x_{lt} = \tau_t + \gamma B_{lt} + \eta_{lt} = \underbrace{\left(\tau_t + g_{2t}\gamma\right)}_{\tilde{\tau}_t} + z_{l10}(g_{1t} - g_{2t})\gamma + \eta_{lt}$$

- Now we cannot directly say only  $z_{l10}$  is the instrument
- Because with two periods,  $g_{1t} g_{2t}$  is not a constant
- Let's further decompose the equation

■ Denote indicator function as  $\mathbf{1}(\cdot)$ , we have:

$$g_{1t} - g_{2t} = \mathbf{1}(t=1)(g_{11} - g_{21}) + \mathbf{1}(t=2)(g_{12} - g_{22})$$

Then first stage becomes:

$$x_{lt} = \tilde{\tau}_t + z_{l10} \mathbf{1}(t=1) \underbrace{(g_{11} - g_{21})\gamma}_{\text{rescaled parameter } \tilde{\gamma}_1} + z_{l10} \mathbf{1}(t=2) \underbrace{(g_{12} - g_{22})\gamma}_{\text{rescaled parameter } \tilde{\gamma}_2}$$

- This is running x on the time FE and two interactions of  $z_{l10}$  and time dummies
- $g_{12} g_{22}$  is the relative industry growth rate (shock)
- What is the underlying research design here?

- Growth rate: policy effect size;
- Initial share: Exposure to some policy
- Whether locations with more industry 1, experience different changes in *x* following shocks whose effect depends on industry sizes
- More clear if we consider period 1 as some pre-period
- Then we can set  $g_{11} g_{21} = 0$ : Before policy/after policy
- DID specification!  $\tilde{\gamma}_1$  = 0  $\Rightarrow$  parallel pre-trend

- Assume that we have K industries and one period, stack all variables to matrix
- Let  $M_D = I D(D'D)^{-1}D'$  be the annihilator matrix,  $X^{\perp} = M_D X$
- $\blacksquare$  Z is share and G is shock

#### Proposition 1 in PSS(2020)

We define Bartik and GMM esimator using industry shares as instruments:

$$\hat{\beta}_{Bartik} = \frac{B'Y^{\perp}}{B'X^{\perp}}, \hat{\beta}_{GMM} = \frac{X^{\perp'}ZWZ'Y^{\perp}}{X^{\perp'}ZWZ'X^{\perp}}$$

If 
$$W = GG'$$
, then  $\hat{\beta}_{Bartik} = \hat{\beta}_{GMM}$ 

- Bartik IV is equivalent to GMM estimator with local industry shares as instruments and national growth rate variance as weights
- Combined just-identified IV vs. Multiple over-identified IV
- The results can be extended to K industries and T periods case

- Asymptotic in location dimension:  $L \to \infty$ , with fixed T, K
- Asymptotic in other dimensions (and different research designs) are discussed in the next paper
- Assumption 1: Relevance
- Assumption 2 (Strict Exogeneity):  $E[\epsilon_{lt}z_{lk0}|D_{lt}] = 0, \forall k \text{ with } g_k \neq 0$

#### Proposition 2 in PSS(2020)

Given assumption 1 and 2,

$$plim\hat{\beta}_{Bartik} - \beta_0 = 0$$

Generally, when is Assumption 2 plausible?

- Initial industry share is mean independent of unobserved outcome levels Wrong!
- Initial industry share is mean independent of unobserved outcome changes
   Plausible
- Keep in mind, when using Bartik IV Either control for location+time FE, or use growth variable as y!

#### When is Assumption 2 plausible?

- This is an "exposure design" (similar to DID)
- Different exposures of locations to national industry-level shocks affect outcomes only through changing x
- There is no systematic difference in terms of unobserved local shocks for places with different exposures (parallel trend)
- Think of Shanghai, Hong Kong and Shenyang, Wuhan
  - SH, HK are more involved in finance industry than SY, WH
  - If a financial crisis happens, SH, HK are more exposed
  - We have to assume that there is no other unobserved shocks hitting SH, HK and SY, WH differently
  - The trend of economic situations (without crisis shock) should be parallel

- Bartik IV is a combination of many industries (Black box)
- Which industry is driving the results?

 We can decompose it into a combination of just-identified estimates on each instrument (for each industry)

#### Proposition 3 in PSS(2020)

We can write

$$\hat{\beta}_{Bartik} = \sum_{k} \hat{\alpha}_{k} \hat{\beta}_{k}$$

where

$$\hat{\beta}_{k} = (Z'_{k}X^{\perp})^{-1}Z'_{k}Y^{\perp}, \hat{\alpha}_{k} = \frac{g_{k}Z'_{k}X^{\perp}}{\sum_{k'}g_{k'}Z'_{k'}X^{\perp}}$$

- We construct a single instrument for each industry  $B_k = z_{lk0}g_k$
- $\hat{\beta}_k$  is IV estimator for each instrument k
- $\hat{\alpha}_k$  is called Rotemberg weight
- The Rotemberg weight means how important this single industry is
- If  $\hat{\alpha}_k$  is large, misspecification on this industry is dangerous
- lacksquare If  $\hat{lpha}_k$  is small, misspecification on this industry could be fine
- In practice, report industries with the highest weights

#### Tips

- This decomposition is different from the main GMM interpretation
- Bartik IV and GMM equivalence is discussed in a joint estimation context
- Bartik IV is equivalent to a joint GMM with shares as IVs (in one regression)
- Bartik IV decomposition means Bartik IV can be decomposed to a combination of K separately estimated IV estimators
- We run these IV regs one by one (for each industry share), then take weighted average of each regression coefficient  $\hat{\beta}_k$

## Goldsmith-Pinkham, Sorkin, and Swift (2020): Heterogeneous TE

- In a restricted heterogeneous effect case: Bartik IV is a combination of location level treatment effect
- Weights can be negative: lead the estimator to be uninterpretable
- For single industry share IV:
   We need an assumption similar to monotonicity in Imbens and Angrist (1994)
- For combined Bartik IV: Monotonicity for each single instrument is not enough
- In general, Bartik IV does not have a LATE interpretation

## Goldsmith-Pinkham, Sorkin, and Swift (2020): Heterogeneous TE

- You will find similar things in the forthcoming lectures when we discuss complicated DID designs
- When treatment effect patterns become more and more complicated
- For instance dynamic, heterogeneous...
- You can hardly identify meaningful causal parameters using simple regressions
- Is this just coincidence?
- No. This is an intrinsically problem. Think about why

- Now we have introduced an econometrics analysis of the Bartik IV
- What should we do in our empirical research if we want to interpret Bartik IV in the framework of Goldsmith-Pinkham, Sorkin, and Swift (2020)?
- First, remember, always add in location and time FE
- Second, focus on industries with high Rotemberg weights

#### Some tests you can implement

- Test 1: Correlations of controls and industry compositions
- $\blacksquare$  Assume that there are some covariates predicting changes in y not through x
- Test whether these location covariates are correlated with the industry shares
- Since industry shares need to affect y only through changes in x
- This is a balance test
- Example: *y* is employment; *x* is wage; *z* is manufacturing share; covariate *d* is immigrant share
- A suggestion from GSS: control for higher level shares

- Test 2: Test for pre-trends if you have pre-shock period
- In specification with pre-period, you are doing DID
- Initial shares are local policy exposure; Growth rates are policy size
- Check pre-trends for both overall Bartik IV and single industry IV with high weight
- Whether locations with high shares of a main industry is different to locations with low shares in trends

- Test 3: Overidentification Tests
- The main equivalence result tells us Bartik IV is an over-identified GMM
- Let's run overidentification test to check the validity of the bundle of share instruments
- If it is rejected, there are two possibilities
- Either your instruments are not exogenous (misspecification)
- Or there is heterogeneous treatment effect etc...
- This is not so recommended

# Borusyak, Hull, and Jaravel (2022): Shift as IV

- We have already investigated Goldsmith-Pinkham, Sorkin, and Swift (2020)
- They interpret the share part as IV and the shift part as weight
- Another framework is proposed by Borusyak, Hull, and Jaravel (2022)
- In contrast, they interpret the shift part as IV and the share part as weight
- The identification assumption then becomes the "random assignment of shocks"

# Borusyak, Hull, and Jaravel (2022): Settings

Assume that we have the following shift-share IV:

$$z_I = \sum_k s_{Ik} g_k, \quad k = 1, 2, ..., K$$

- $\bullet$   $s_{lk}$  is the share of industry k in location l
- $lackbox{ } g_k$  is the national shift for industry k
- We seek to estimate parameter  $\beta$  in the following regression:

$$y_I = \beta x_I + w_I^{\prime} \gamma + \epsilon_I$$

- w is the set of controls
- A valid instrument satisfies moment condition:  $E[\sum_{l} z_{l} \epsilon_{l}] = 0$

- Now we derive the equivalence between the original regression and a shock-level regression
- Plug the definition of SSIV into the moment condition:

$$E\left[\sum_{I}z_{I}\epsilon_{I}\right]=E\left[\sum_{I}\sum_{k}s_{Ik}g_{k}\epsilon_{I}\right]$$

■ We exchange the order of the summation and have:

$$\begin{split} E[\sum_{l} z_{l} \epsilon_{l}] &= E[\sum_{k} \sum_{l} s_{lk} g_{k} \epsilon_{l}] = E[\sum_{k} g_{k} \sum_{l} s_{lk} \epsilon_{l}] \\ &= E[\sum_{k} g_{k} (\frac{\sum_{l} s_{lk} \epsilon_{l} \cdot \sum_{l} s_{lk}}{\sum_{l} s_{lk}})] = E[\sum_{k} s_{k} g_{k} \overline{\epsilon}_{k}] \end{split}$$

- $s_k = \sum_l s_{lk}$  is the sum of shares of industry k for all locations
- $s_k = 1$  in many common examples
- lacksquare  $ar{\epsilon}_k = rac{\sum_l s_{lk} \epsilon_l}{\sum_l s_{lk}}$  is a weighted average of unobserved terms
- lacksquare It transforms the original  $\epsilon$  from location-level  $\emph{I}$  to industry-level  $\emph{k}$

- Therefore, it transforms the identification assumption from I level to k level
- Now assume that we want to identify the effect of U.S. tariff on employment in China
- What is the research design here?
- $lue{}$  Can you interpret the identification assumption at k level?

- The industry demand shocks  $g_k$  must be orthogonal with the industry-level unobservables  $\bar{\epsilon}_k$ , the average local supply shocks in different regions weighted by industry size
- Industries experiencing a rise in tariff should not face systematically different labor supply shocks in their primary markets
- Assume a U.S. tariff hits steel industry in China, which hits Hebei hard
- We should expect no labor supply shocks in Hebei, such as a change of enrollment quota in Gaokao at the same time

# Borusyak, Hull, and Jaravel (2022): Shock-level Equivalence

Now we have the following proposition

### Proposition 1 in BHJ(2022)

The SSIV estimator  $\hat{\beta}$  equals the second-stage coefficient from a  $s_k$ -weighted shock-level IV regression that uses the shocks  $g_k$  as the instrument in estimating

$$\bar{y}_k = \alpha + \beta \bar{x}_k + \bar{\epsilon}_k$$

where  $\bar{v} = \frac{\sum_{l} s_{lk} v_{l}}{\sum_{l} s_{lk}}$  denotes an exposure-weighted average of a variable  $v_{l}$ 

 This proposition 1 establishes the equivalence between the original and the shock-level regressions

## Borusyak, Hull, and Jaravel (2022): Shock-level Equivalence

- We establish the consistency of this estimator under two assumptions:
  - Assumption 1:  $E[g_k|\bar{\epsilon},s] = \mu$ , quasi-random shock assignment
  - Assumption 2:  $E[\sum_k s_k^2] \to 0$ ,  $Cov[g_k, g_{k'}|\bar{\epsilon}, s] = 0$ , many uncorrelated shocks industries should not be too concentrated

### Proposition 3 in BHJ(2022)

Suppose Assumptions 1-2 and some other regularity conditions hold, we have:  $\hat{\beta} \xrightarrow{p} \beta$ 

Identification is valid when shocks are random

- The first empirical suggestion is about the inference of the std err
- Adao, Kolesár, and Morales (2019) show that the traditional inference is incorrect since samples in the SSIV setting are intrinsically not i.i.d.
- Because there is common shock components  $g_k$  and  $\nu_k$  in  $\epsilon_l$  and  $z_l$
- $lackbox{\bullet} \epsilon_I$  and  $z_I$  are mechanically correlated across observations
- The correlations are large for locations with similar industry shares

- Borusyak, Hull, and Jaravel (2022) show that the shock-level regression does not suffer from this
- You can directly use the traditional std err and CI estimated here
- A stata package can help you run this shock-level regression: ssaggregate

- The second empirical suggestion is about the descriptive test for IV validity
- lacksquare A simple balance test is to regress some pre-determined control  $r_l$  on IV  $z_l$
- $ightharpoonup r_l$  can be location level GDP, population etc...
- This can be combined with the Oster bound method
- lacksquare Another balance test is to start from a industry shock-level confounder  $r_k$
- Then construct location-level average  $r_l = \sum_k s_{lk} r_k$
- Then run this average  $r_l$  on IV  $z_l$

- Another possible way to implement the balance test is to transform everything to k level
- We can aggregate location l level confounder  $r_l$  to industry k level by  $r_k = \frac{\sum_l s_{lk} r_l}{\sum_l s_{lk}}$
- Then we run this  $r_k$  on shock  $g_k$
- Personally, I think this is more important than previous two
- Because it directly test the main assumption

### Comparison of the Two Frameworks

- We have introduced two frameworks to understand Bartik IV
- The first is Goldsmith-Pinkham, Sorkin, and Swift (2020)
  - Equivalence: GMM with share as instrument, shift as weight
  - Research design: Exposure DID
  - Assumption: Locations with different shares have parallel trend
- The second is Borusyak, Hull, and Jaravel (2022)
  - Equivalence: Shock-level regression, shift as instrument, share as weight
  - Research design: Randomly assigned shocks
  - Assumption: Industries with large shocks do not have systematically different unobserved shocks in their primary market (location)

### Comparison of the Two Frameworks

- When should we use these two frameworks?
- We should consider Goldsmith-Pinkham, Sorkin, and Swift (2020) when
  - Exogeneity comes from share
  - Emphasize differential exposure to common shocks (DID design)
  - Fixed small number of industries  $(K = K^*, L \rightarrow \infty)$
  - Focus on shock exposure of several specific industries
  - Have some exposure shares tailored to the specific policy question
- We should consider Borusyak, Hull, and Jaravel (2022) when
  - Exogeneity comes from shift (shock)
  - We believe shocks are randomly assigned
  - Fixed small number of locations  $(K \to \infty, L = L^*)$
  - Whenever the second-stage error  $\epsilon_{lk}$  has a shift-share structure Mechanical correlation between Bartik IV and this error  $\epsilon_{lk} = \sum_k s_{lk} \epsilon_k$

## Application: Autor, Dorn, and Hanson (2013)

- The paper report this week is Autor, Dorn, and Hanson (2013)
- Impact of import from China on the local labor markets in the U.S., "China Syndrome"
- Goldsmith-Pinkham, Sorkin, and Swift (2020) and Borusyak, Hull, and Jaravel (2022) use this paper as an example
- To show how to apply their frameworks
- Please not only read the original paper, but also read the corresponding part in Goldsmith-Pinkham, Sorkin, and Swift (2020) and Borusyak, Hull, and Jaravel (2022)

### Conclusion

- Bartik IV is constructed in a shift-share style
- It is widely used in spatial economics for trade and migration
- We illustrate two frameworks to understand it
  - Goldsmith-Pinkham, Sorkin, and Swift (2020)
  - Borusyak, Hull, and Jaravel (2022)
- When to use which framework really depends on the setting of our research

### Conclusion

For Goldsmith-Pinkham, Sorkin, and Swift (2020)

- Bartik IV is equivalent to GMM with shares as instruments
- We should always control for location/time FE, or use change variables
- Bartik IV is similar to a policy exposure design, with initial shares as the exposures
- We can decompose Bartik IV to be weighted averages of single share instruments
- The Rotemberg weights show the importance of each single industry

### Conclusion

For Borusyak, Hull, and Jaravel (2022)

- Bartik IV is equivalent to a shock-level regression with shifts as instruments
- The research design is based on the assumption of a series of randomly assigned shocks
- Be careful about the inference of the std err due to the serial correlation nature of the DGP ⇒ A transformation to shock-level regression can avoid this issue

### References

- Adao, Rodrigo, Michal Kolesár, and Eduardo Morales. 2019. "Shift-share Designs: Theory and Inference." *The Quarterly Journal of Economics* 134 (4):1949–2010.
- Autor, David H, David Dorn, and Gordon H Hanson. 2013. "The China Syndrome: Local Labor Market Effects of Import Competition in the United States." *American Economic Review* 103 (6):2121–2168.
- Borusyak, Kirill, Peter Hull, and Xavier Jaravel. 2022. "Quasi-experimental Shift-share Research Designs." *The Review of Economic Studies* 89 (1):181–213.
- Card, David. 2009. "Immigration and Inequality." American Economic Review 99 (2):1-21.
- Goldsmith-Pinkham, Paul, Isaac Sorkin, and Henry Swift. 2020. "Bartik Instruments: What, When, Why, and How." *American Economic Review* 110 (8):2586–2624.